

SEEC Stats Toolbox

Want to broaden your stats knowledge? Unsure of what you can do with your data? Still developing your proposal?

Join us for the monthly **SEEC Stats Toolbox** seminars where we introduce you to statistical methods that are useful for ecologists, environmental and conservation scientists.

Our next seminar:



Topic: **Species occupancy models**

Who: Res Altwegg

When: Thursday 31 May (1-2pm)

Where: John Day LT3

More details: www.seec.uct.ac.za

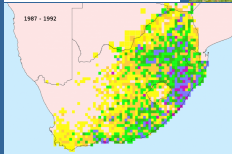
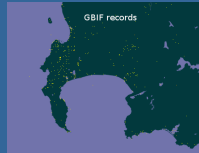
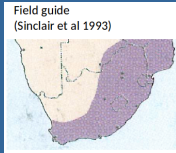


SEEC - Statistics in Ecology, Environment and Conservation

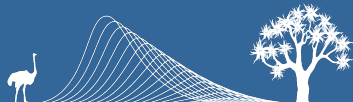
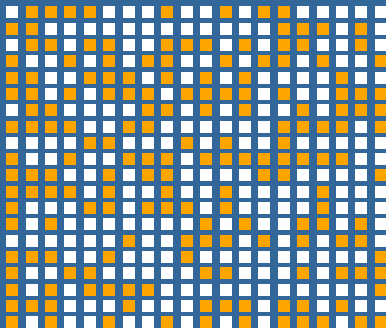


Occupancy

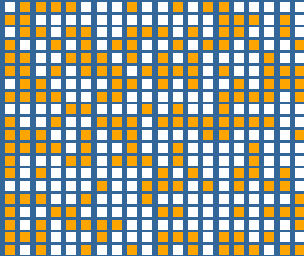
- ▶ Where a species occurs; which of a set of suitable patches are occupied; what determines where a species can live...
- ▶ (Metapopulation) ecology, conservation, red-listing



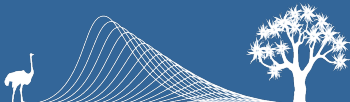
Occupancy: the proportion of sites occupied by a species



Occupancy: the proportion of sites occupied by a species

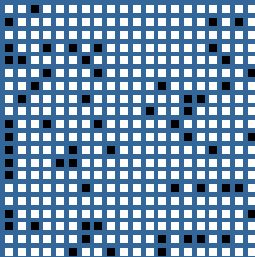
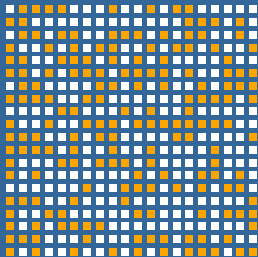


- ▶ Occupancy: $\psi = \frac{\text{occupied}}{\text{total}}$
- ▶ $\text{logit}(\psi) = f(\text{covariates})$



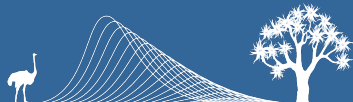
The species is not detected in all occupied cells

Detection probability $p < 1$

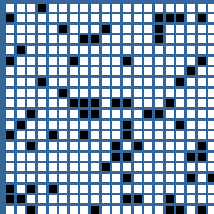
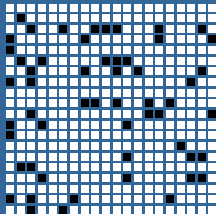
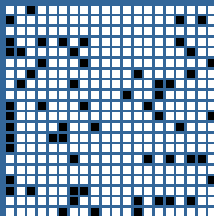
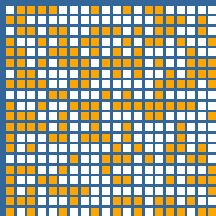


'Naive approach':

- ▶ $\Psi \times p = \frac{\text{occupied}}{\text{total}}$
- ▶ $\text{logit}(\Psi \times p) = f(\text{covariates})$



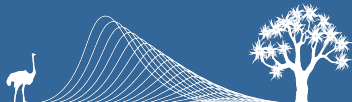
The species is not detected in all occupied cells



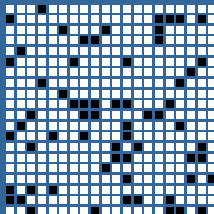
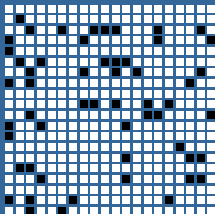
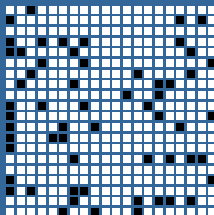
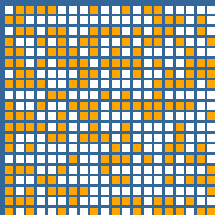
Repeated sampling

Assumptions:

- ▶ Closure (no colonisation or extinction)
- ▶ No false detections



The species is not detected in all occupied cells



Survey histories:

1 = detected

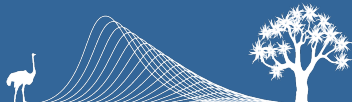
0 = not detected

▶ (1,1) 000

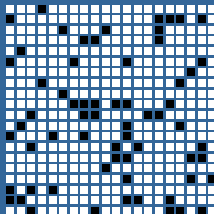
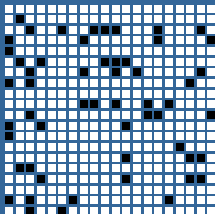
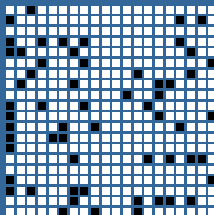
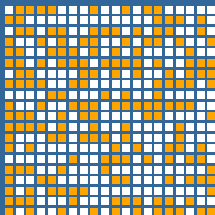
▶ (1,3) 100

▶ (2,1) 101

▶ (1,9) 000



The species is not detected in all occupied cells



Survey histories:

1 = detected

0 = not detected

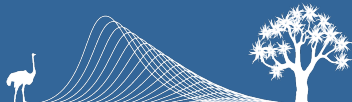
▶ (1,1) 000

▶ (1,3) 100

▶ (2,1) 101

▶ **(1,9) 000**

How many occupied cells
have no detections?



A model for the detections

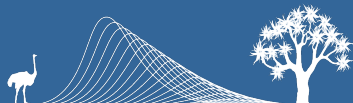
Ψ = probability of a cell to be occupied

p = probability of detecting the species given that the cell is occupied

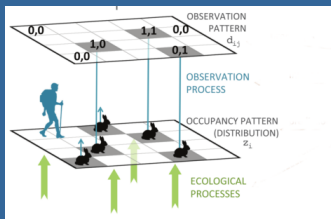
K = number of visits to each site

y_i = number of detections at site i

$$\begin{aligned} Pr(Y = y_i) &= \Psi \binom{K}{y_i} p^{y_i} (1 - p)^{K - y_i}, y_i > 0 \\ &= \Psi (1 - p)^K + (1 - \Psi), y_i = 0 \end{aligned}$$



A hierarchical model



Guillera-Arroita 2017

Ψ_i = probability that site i is occupied

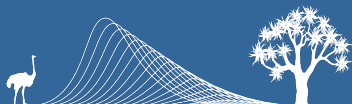
z_i = true occupancy at site i : 1 = occupied, 0 = not occupied

p_{ij} = prob of detecting the species at site i during survey j

y_{ij} = detection (1) or non-detection (0) at site i during survey j

$$z_i | \Psi_i \sim \text{Bernoulli}(\Psi_i)$$

$$y_{ij} | z_i, p_{ij} \sim \text{Bernoulli}(z_i p_{ij})$$



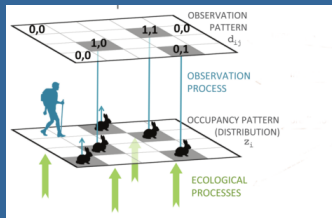
A hierarchical model

Ecological process:

$$z_i | \Psi \sim \text{Bernoulli}(\Psi)$$

Observation process:

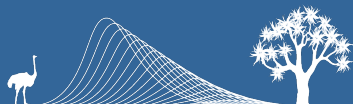
$$y_{ij} | z_i, p \sim \text{Bernoulli}(z_i p)$$



```
model {  
  for (i in 1:nsites) {  
    z[i] ~ dbern(psi)  
  
    p.eff[i] <- z[i] * p  
    for (j in 1:nvisits) {  
      y[i,j] ~ dbern(p.eff[i])  
    } #j  
  } #i
```

```
# Priors  
psi ~ dunif(0, 1)  
p ~ dunif(0, 1)
```

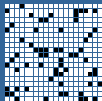
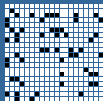
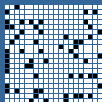
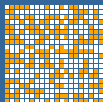
```
# Derived quantities  
occ.fs <- sum(z[])  
}
```



Preparing the data

$$\Psi = 0.5$$

$$p = 0.3$$



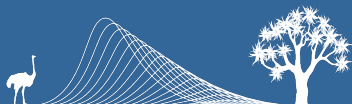
```
> head(y)
```

	detected1	detected2	detected3
1	0	0	0
2	0	0	0
3	0	1	1
4	0	0	0
5	0	0	0
6	1	1	0

‘Naive’ occupancy:

$$\frac{126}{400} = 0.32$$

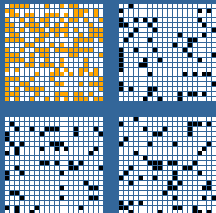
```
> dim(y)
[1] 400 3
```



Preparing inputs for JAGS

$$\psi = 0.5$$

$$p = 0.3$$



'Naive' occupancy:

$$\frac{126}{400} = 0.32$$

```
library(jagsUI) # requires JAGS
```

```
occ.data <- list(y = y, nsites = nrow(y),  
                 nvisits = ncol(y))
```

```
# Initial values
```

```
zst <- apply(y, 1, max)
```

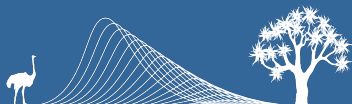
```
inits <- function() list(z = zst)
```

```
# Parameters monitored
```

```
params <- c("psi", "p", "occ.fs")
```

```
# MCMC settings
```

```
nc <- 3; ni <- 5000; nb <- 2000
```

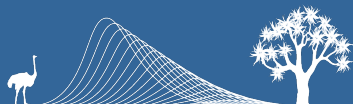


Fitting the model to the data

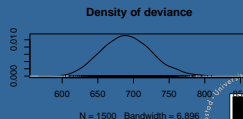
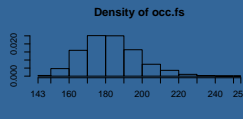
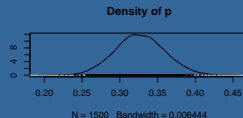
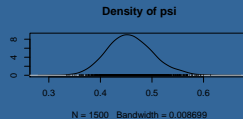
```
> out.occ <- jags(occ.data, inits, params, "occ.txt",  
  n.chains=nc, n.iter=ni, n.burn = nb)
```

```
> out.occ$summary
```

	mean	sd	Rhat	n.eff
psi	0.4578	0.0448	1.0028	752
p	0.3274	0.0331	1.0016	1675
occ.fs	182.8655	15.2283	1.0016	1312
deviance	690.6184	35.3438	1.0016	1276

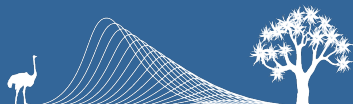
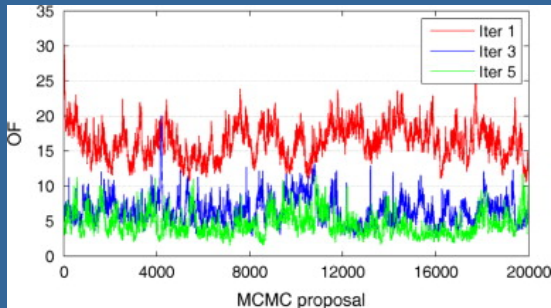


```
> plot(out.occ)
```



Bad example

If your chains look like this, don't trust the output!!



Covariate modelling

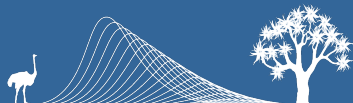
Want to know how occupancy and detection vary among sites, i , and visits, j .

$$\text{logit}(\Psi_i) = \beta_0 + \beta_1 x_{i1} + \dots + \beta_U x_{iU}$$

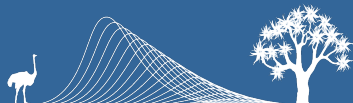
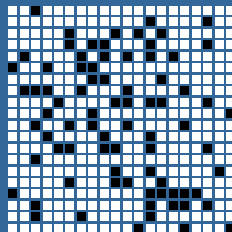
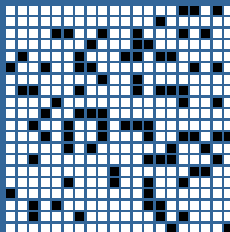
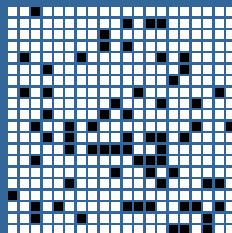
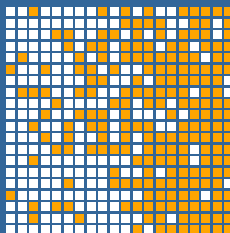
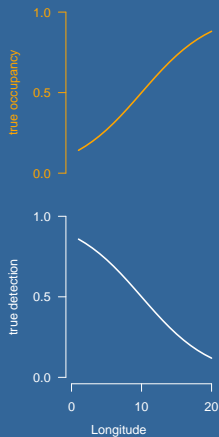
$$\text{logit}(p_{ij}) = \beta_0 + \beta_1 x_{i1} + \dots + \beta_U x_{iU} + \beta_{U+1} y_{ij1} + \dots + \beta_{U+V} y_{ijV}$$

U site-level covariates: x_{i1}, \dots, x_{iU}

V survey-specific covariates: y_{ij1}, \dots, y_{ijV}



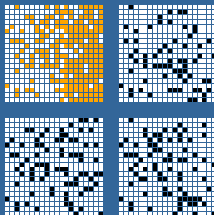
Occupancy and detection vary in space



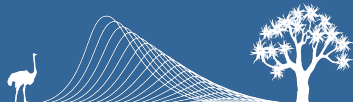
Occupancy and detection vary in space

$$\text{logit}(\Psi_i) = \beta_1^\Psi + \beta_2^\Psi \text{long}_i$$

$$\text{logit}(p_{ij}) = \beta_1^p + \beta_2^p \text{long}_i$$



```
model {  
  # Ecological model  
  for (i in 1:nsites) {  
    z[i] ~ dbern(psi[i])  
  
    # Observation model  
    p.eff[i] <- z[i] * p[i]  
    for (j in 1:nvisits) {  
      y[i,j] ~ dbern(p.eff[i])  
    } #j  
  } #i  
  
  # covariates  
  for (i in 1:nsites){  
    logit(psi[i]) = beta.psi[1] + beta.psi[2]*long[i]  
    logit(p[i]) = beta.p[1] + beta.p[2] * long[i]  
  }  
  
  # Priors  
  for (b in 1:2){  
    beta.psi[b] ~ dnorm(0, 0.01)  
    beta.p[b] ~ dnorm(0, 0.01)  
  }  
}
```



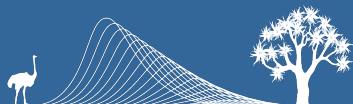
Occupancy and detection vary in space

```
occ.data <- list(y = y, nsites = nrow(y),  
                nvisits = ncol(y), long=long)
```

```
inits <- function() list(z = zst, beta.psi=runif(2,-3,3),  
                        beta.p=runif(2,-3,3))
```

```
params <- c("beta.psi", "beta.p", "occ.fs")
```

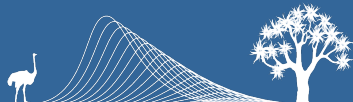
```
out.occ.cov <- jags(occ.data,inits,params,"occ_cov.txt",  
                  n.chains=3, n.iter=5000, n.burn = 2000)
```



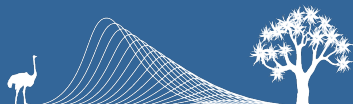
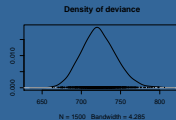
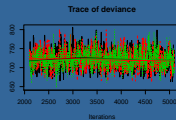
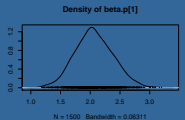
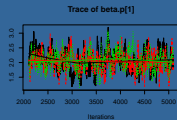
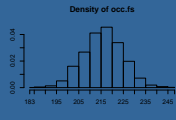
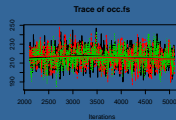
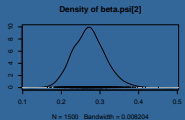
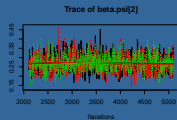
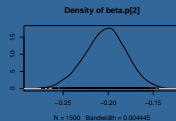
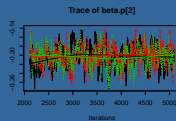
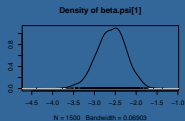
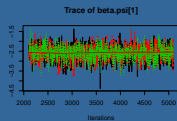
Occupancy and detection vary in space

```
> out.occ.cov$summary
```

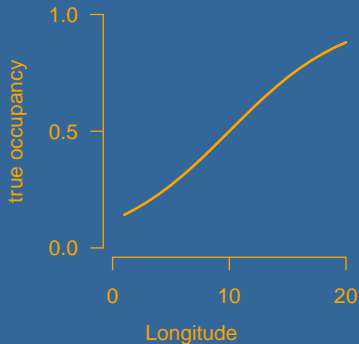
	mean	sd	2.5%	97.5%	Rhat	n.eff
beta.psi[1]	-2.59	0.350	-3.31	-1.93	1	2674
beta.psi[2]	0.27	0.042	0.20	0.36	1	2755
beta.p[1]	2.07	0.320	1.46	2.72	1	1340
beta.p[2]	-0.20	0.023	-0.25	-0.16	1	1185
deviance	722.23	22.120	681.30	768.56	1	4385



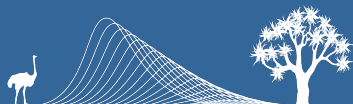
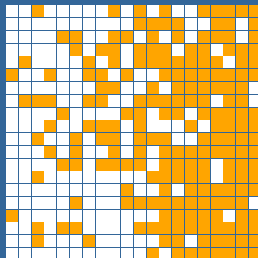
Check convergence!



Estimated occupancy probability



$$\text{logit}(\Psi_i) = \beta_0 + \beta_1 \text{long}_i$$

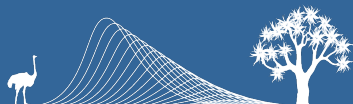


Estimated occupancy probability

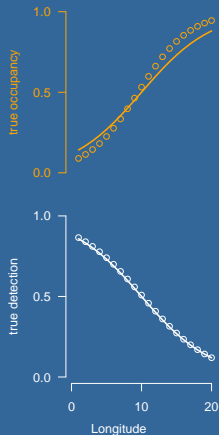
$$\text{logit}(\Psi_i) = \beta_0 + \beta_1 \times \text{long}_i$$

$$\Psi_i = \frac{1}{1 + e^{-(\beta_0 + \beta_1 \times \text{long}_i)}}$$

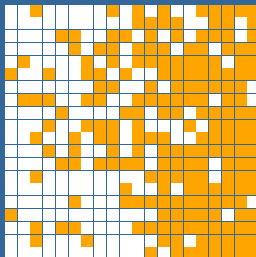
```
new.long <- 1:20  
pr.s <- inv.logit(-2.59 + 0.27 * new.long)  
> pr.s  
[1] 0.089 0.114 0.145 0.182 0.226 0.277 0.334 0.397  
[9] 0.464 0.532 0.599 0.662 0.720 0.772 0.816 0.853  
[17] 0.884 0.909 0.930 0.945
```



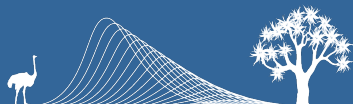
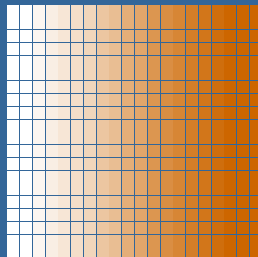
Estimated occupancy probability



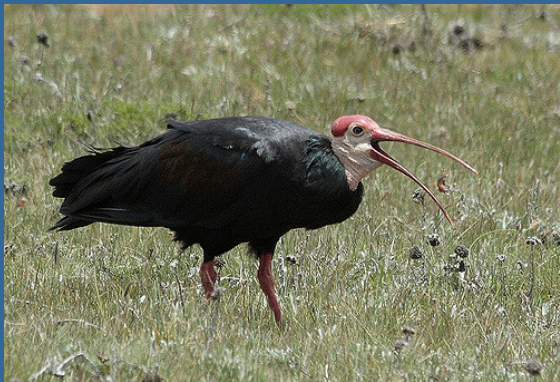
True occupancy



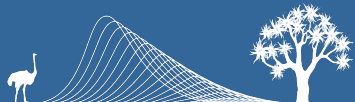
Fitted occupancy



Southern bald ibis range in South Africa



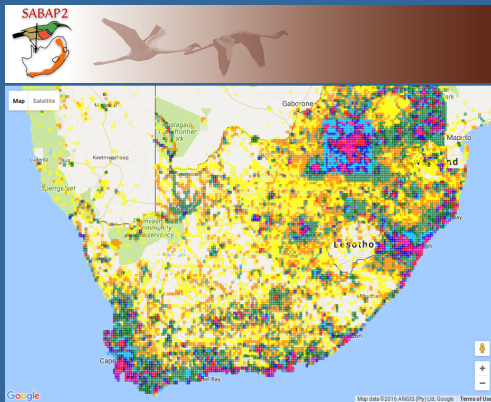
www.flickr.com/photos/12457947@N07/4251701580



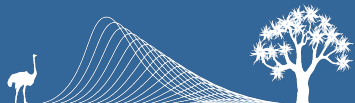
SEEC - Statistics in Ecology, Environment and Conservation



Second Southern African Bird Atlas Project



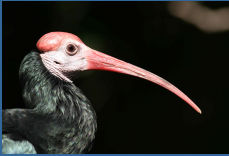
<http://sabap2.adu.org.za/>



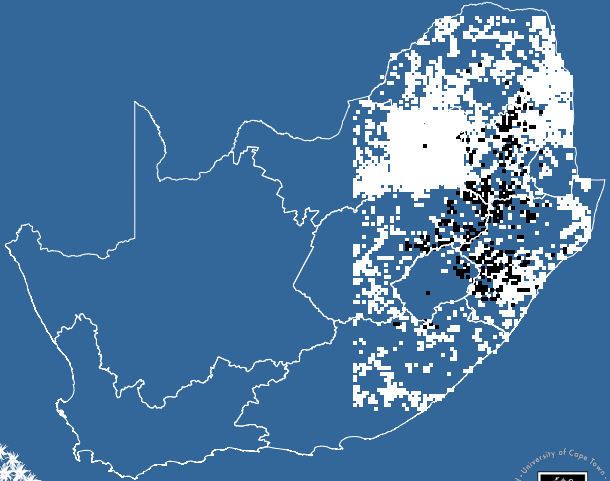
SEEC - Statistics in Ecology, Environment and Conservation



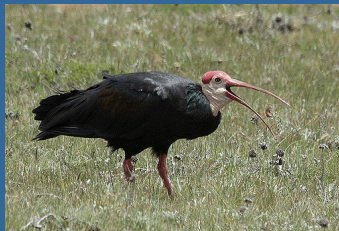
Southern bald ibis



© Peter Ryan

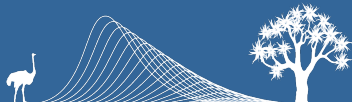


Southern bald ibis



www.flickr.com/photos/12457947@N07/4251701580

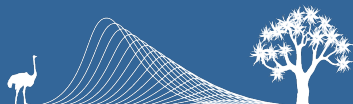
- ▶ Data: 30 June 2015 to 1 July 2017
- ▶ 3220 grid cells $5' \times 5'$
- ▶ 26'619 checklists (1 to 719 per cell)
- ▶ **Site-level covariates:** mean temp coldest month, mean temp warmest month, ratio actual to potential evapotranspiration, wet season intensity
- ▶ **Survey-specific covariates:** $\log(\text{hours observed})$



Preparing the data: long table format

```
> head(bi.m)
```

Pentad	Start_Date	lat	long	Total_hours	Spp
2240_2820	2016-05-28	-22.70833	28.37500	4	0
2240_2820	2015-10-10	-22.70833	28.37500	2	0
2235_2825	2015-10-11	-22.62500	28.45833	2	0
2235_2815	2015-09-25	-22.62500	28.29167	4	0
2240_2815	2015-09-25	-22.70833	28.29167	2	0



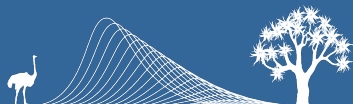
After some data wrangling

```
> y[1:5,1:10]
```

	[,1]	[,2]	[,3]	[,4]	[,5]	[,6]	[,7]	[,8]	[,9]	[,10]
[1,]	0	NA	NA	NA	NA	NA	NA	NA	NA	NA
[2,]	0	NA	NA	NA	NA	NA	NA	NA	NA	NA
[3,]	0	0	0	0	0	0	0	0	0	0
[4,]	0	0	NA	NA	NA	NA	NA	NA	NA	NA
[5,]	0	0	NA	NA	NA	NA	NA	NA	NA	NA

```
> dim(y)
```

```
[1] 3220 719
```



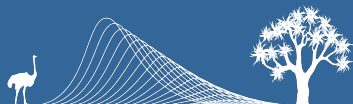
Survey-specific covariates

```
> lhours[1:5,1:10]
```

	[,1]	[,2]	[,3]	[,4]	[,5]	[,6]	[,7]	[,8]	[,9]	[,10]
[1,]	0.69	NA	NA	NA	NA	NA	NA	NA	NA	NA
[2,]	1.39	NA	NA	NA	NA	NA	NA	NA	NA	NA
[3,]	1.61	1.39	1.6	2.1	1.1	0.69	1.8	1.4	0.69	1.4
[4,]	0.69	1.39	NA	NA	NA	NA	NA	NA	NA	NA
[5,]	1.61	0.69	NA	NA	NA	NA	NA	NA	NA	NA

```
> dim(lhours)
```

```
[1] 3220 719
```

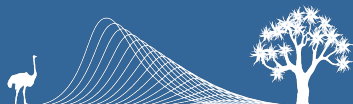


Site-specific covariates

```
> head(MTCO)
      [,1]
[1,] 0.981870
[2,] 0.981870
[3,] 1.041489
[4,] 1.071299
[5,] 1.429016
[6,] 1.429016
```

- ▶ One value per grid cell
- ▶ Covariates scaled to $\bar{x} = 0, s = 1$

```
> dim(MTCO)
[1] 3220    1
```



The model

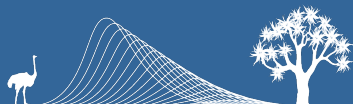
$$z_i | \Psi_i \sim \text{Bernoulli}(\Psi_i)$$

$$y_{ij} | z_i, p_{ij} \sim \text{Bernoulli}(z_i p_{ij})$$

$$\text{logit}(\Psi_i) =$$

$$\beta_1^\Psi + \beta_2^\Psi \text{MTCO}_i + \beta_3^\Psi \text{MTWA}_i + \beta_4^\Psi \text{AET.PET}_i + \beta_5^\Psi \text{Wet.intensity}_i$$

$$\text{logit}(p_{ij}) = \beta_1^P + \beta_2^P \text{Ihours}_{ij}$$

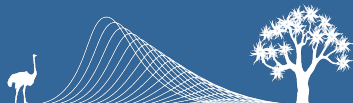


The model

```
model {  
  for (i in 1:nsites) {  
    z[i] ~ dbern(psi[i])  
  
    for (j in 1:ncards[i]) {  
      p.eff[i,j] <- z[i] * p[i,j]  
      y[i,j] ~ dbern(p.eff[i,j])  
    } #j  
  } #i  
  
  # covariates  
  for (i in 1:nsites){  
    logit(psi[i]) = beta.psi[1]  
      + beta.psi[2] * MTCO[i]  
      + beta.psi[3] * MTWA[i]  
      + beta.psi[4] * AET.PET[i]  
      + beta.psi[5] * Wet.Intensity[i]  
  
    for (j in 1:ncards[i]){  
      logit(p[i,j]) = beta.p[1]  
        + beta.p[2] * lhours[i,j]  
    } #j  
  } #i  
}
```

New features:

- ▶ # visits varies among sites
- ▶ multiple covariates
- ▶ observation-level covariates

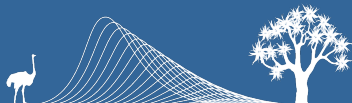


The model

New features:

- ▶ # visits varies among sites
- ▶ multiple covariates
- ▶ observation-level covariates

```
.  
.   
.   
  
# Priors  
for (b in 1:5){  
  beta.psi[b] ~ dnorm(0, 0.01)  
}  
  
for (b in 1:2){  
  beta.p[b] ~ dnorm(0, 0.01)  
}  
}
```



The model

Data:

- ▶ survey histories y
- ▶ site-level covariates
 - ▶ MTCO
 - ▶ MTWA
 - ▶ AET.PET
 - ▶ Wet.intensity
- ▶ observation-level covariates:
lhours
- ▶ # sites: nsites
- ▶ # visits: ncards

Parameters:

- ▶ coefficients for site-level covariates: β_{psi}
- ▶ coefficients for observation-level covariates: β_{p}

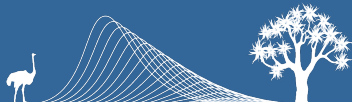
→ need priors

→ need initial values

Unobserved true occupancy

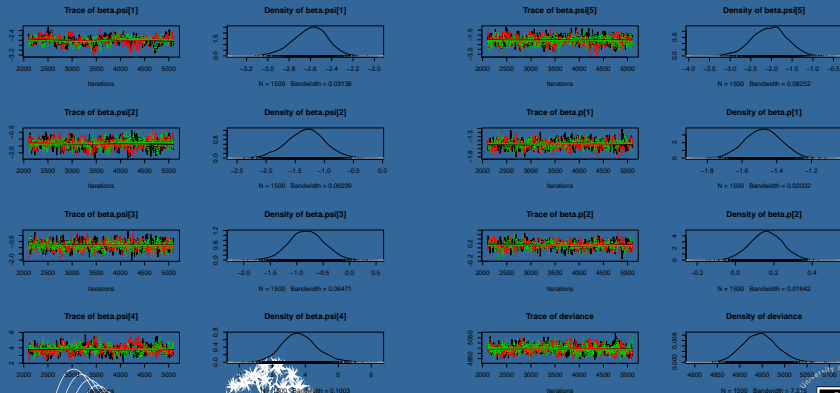
state: z_i

→ need initial values

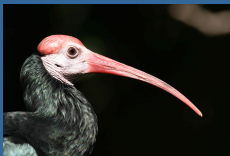


Fit model and check convergence

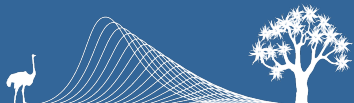
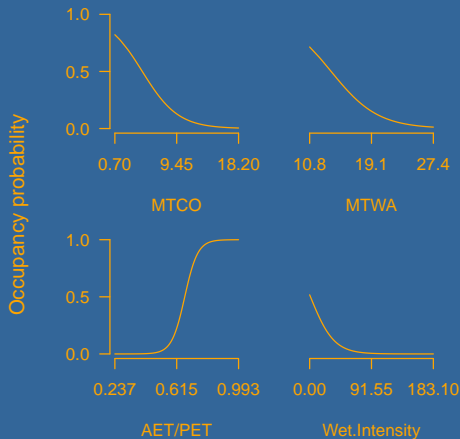
```
out.occ.ib <- jags(occ.data, inits, params, "occ_ibis.txt",  
  n.chains=3, n.iter=5000, n.burn = 2000)  
plot(out.occ.ib)
```



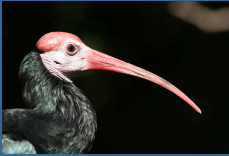
Southern bald ibis



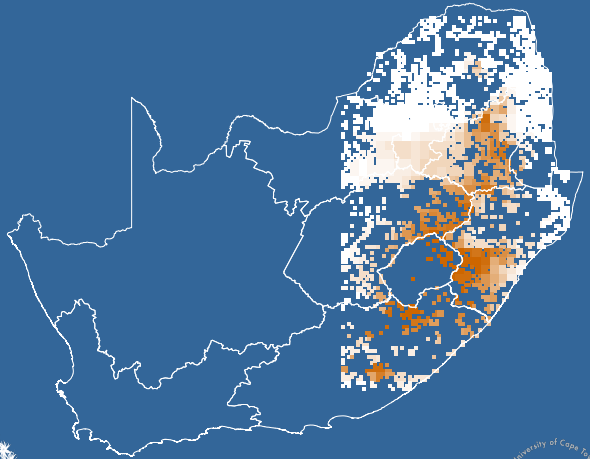
© Peter Ryan



Southern bald ibis

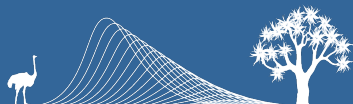


© Peter Ryan



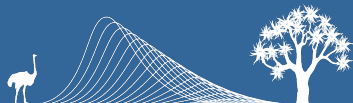
Single-season occupancy models

- ▶ Repeated detection / non-detection data
- ▶ Estimate occupancy and detection process
- ▶ **Key assumptions:** closure, no false detections, surveys are independent, sites are independent
- ▶ Can be fitted using JAGS via R package 'jagsUI'
- ▶ Other software: R package 'unmarked', PRESENCE, MARK



Why go Bayesian?

- ▶ more flexible
- ▶ easy to add random effects
- ▶ spatial autocorrelation
- ▶ can use prior information



Key references

Single-season occupancy models:

- ▶ MacKenzie, D. I., J. D. Nichols, G. B. Lachman, S. Droege, J. A. Royle, and C. A. Langtimm. 2002. Estimating site occupancy rates when detection probabilities are less than one. *Ecology* 83: 2248-2255.
- ▶ MacKenzie, D. I., J. D. Nichols, J. A. Royle, K. H. Pollock, L. L. Bailey, and J. E. Hines. 2017. *Occupancy Estimation and Modeling: Inferring Patterns and Dynamics of Species Occurrence*. Academic Press.
- ▶ Guillera-Aroita, G. 2017. Modelling of species distributions, range dynamics and communities under imperfect detection: advances, challenges and opportunities. *Ecography* 40:281295.

Occupancy models in BUGS:

- ▶ Kéry, M., and M. Schaub. 2012. *Bayesian Population Analysis using WinBUGS: A hierarchical perspective*. Academic Press.
- ▶ Kéry, M., and J. A. Royle. 2016. *Applied Hierarchical Modeling in Ecology*. Academic Press.

