

SEEC STATS TOOLBOX

WANT TO BROADEN YOUR STATS KNOWLEDGE? UNSURE OF WHAT YOU CAN DO WITH YOUR DATA? STILL DEVELOPING YOUR PROPOSAL?

Join us for the monthly SEEC Stats Toolbox seminars where we introduce statistical methods that are useful for ecologists, environmental and conservation scientists.

Our next seminar:

Topic: *Dynamic occupancy models*

Who: Res Altwegg & David Maphisa

When: Thursday 28 November, 13h00 - 14h00

Where: PD Hahn LT4 (Level 6)



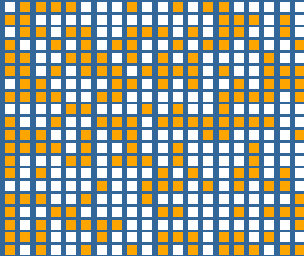
SEEC - Statistics in Ecology, Environment and Conservation



UNIVERSITY OF CAPE TOWN
IYUNIVERSITHI YASIKAPA - UNIVERSITEIT VAN KAAPSTAD

Visit www.seec.uct.ac.za/stats-toolbox-seminars for more information

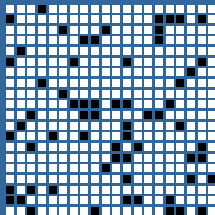
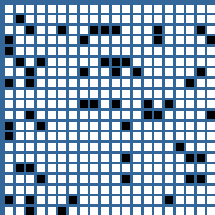
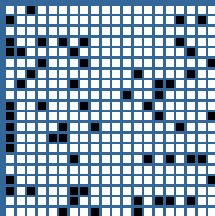
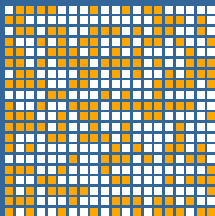
Occupancy: the proportion of sites occupied by a species



- ▶ Occupancy: $\Psi = \frac{\text{occupied}}{\text{total}}$
- ▶ $\text{logit}(\Psi) = f(\text{covariates})$



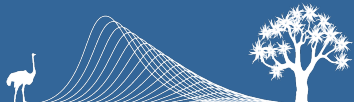
The species is not detected in all occupied cells



Repeated sampling

Assumptions:

- ▶ Closure (no colonisation or extinction)
- ▶ No false detections



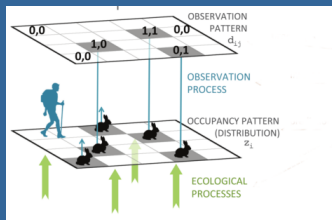
A hierarchical model

Ψ_i = probability that site i is occupied

z_i = true occupancy at site i : 1 = occupied, 0 = not occupied

p_{ij} = prob of detecting the species at site i during survey j

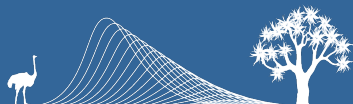
y_{ij} = detection (1) or non-detection (0) at site i during survey j



Guillera-Arroita 2017

$$z_i | \Psi_i \sim \text{Bernoulli}(\Psi_i)$$

$$y_{i,j} | z_i, p_{i,j} \sim \text{Bernoulli}(z_i p_{i,j})$$



Covariate modelling

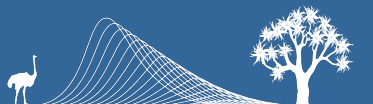
Want to know how occupancy and detection vary among sites, i , and survey, j .

$$\text{logit}(\Psi_i) = \alpha_0 + \alpha_1 x_{i1} + \dots + \alpha_U x_{iU}$$

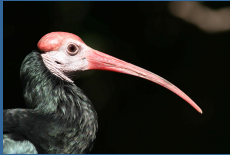
$$\text{logit}(p_{ij}) = \beta_0 + \beta_1 x_{i1} + \dots + \beta_U x_{iU} + \beta_{U+1} y_{ij1} + \dots + \beta_{U+V} y_{ijV}$$

U site-level covariates: x_{i1}, \dots, x_{iU}

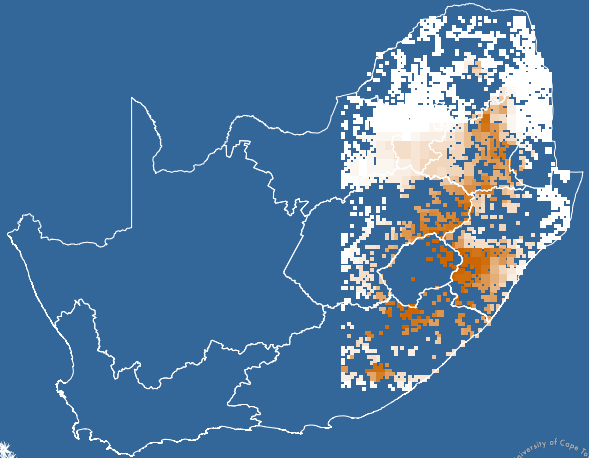
V survey-specific covariates: y_{ij1}, \dots, y_{ijV}



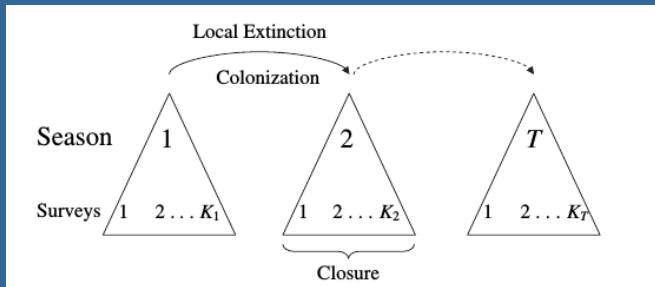
Southern bald ibis



© Peter Ryan

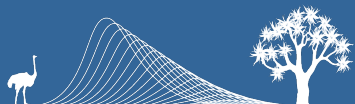


Dynamic occupancy models

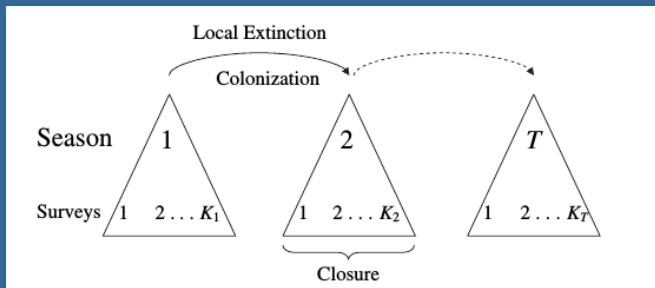


$$z_{i,t} | \Psi_{i,t} \sim \text{Bern}(\Psi_{i,t})$$

$$y_{i,t,j} | z_{i,t}, p_{i,t,j} \sim \text{Bernoulli}(z_i \times p_{i,t,j})$$

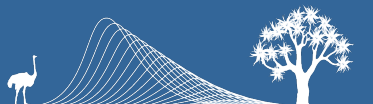


Dynamic occupancy models

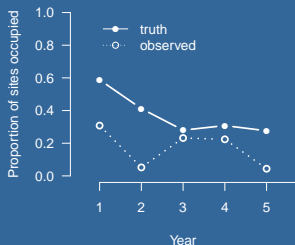


$$\text{logit}(\Psi_{i,1}) = \alpha_0 + \alpha_1 x_{i1} + \dots + \alpha_{UX} x_{iU}$$

$$\Psi_{i,t} | z_{i,t-1} = z_{i,t-1} \times (1 - \epsilon_{i,t-1}) + (1 - z_{i,t-1}) \times \gamma_{i,t-1}, \text{ for } t > 1$$



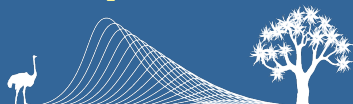
Preparing the data



```
> head(yy)
      [,1] [,2] [,3] [,4]      [,9] [,10]
[1,]    0    1    1    1    ...    1    0
[2,]    0    0    0    0    ...    0    0
[3,]    0    0    0    0    ...    0    0
[4,]    0    0    0    0    ...    0    0
[5,]    0    0    0    0    ...    0    0
[6,]    0    0    0    0    ...    0    0
```

```
> dim(yy)
[1] 250 10
```

- ▶ 250 sites
- ▶ 5 seasons
- ▶ 2 surveys / season
- ▶ $\Psi_1 = 0.6$



Preparing the data

```
> library(unmarked)
> simUMF <- unmarkedMultFrame( y = yy,
+   yearlySiteCovs = list(year = year),
+   numPrimary=5)
> summary(simUMF)
unmarkedFrame Object
```

250 sites

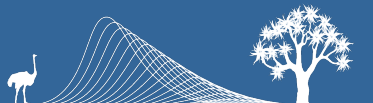
Maximum number of observations per site: 10

Mean number of observations per site: 10

Number of primary survey periods: 5

Number of secondary survey periods: 2

Sites with at least one detection: 136



Preparing the data

Tabulation of y observations:

```
0    1
2242 258
```

Yearly-site-level covariates:

year

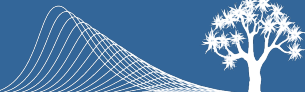
01:250

02:250

03:250

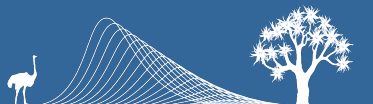
04:250

05:250



Fitting the model to the data

```
> m0 <- colext(psiformula= ~1,  
+             gammaformula = ~ 1,  
+             epsilonformula = ~ 1,  
+             pformula = ~ 1,  
+             data = simUMF)
```



Looking at the output

```
> summary(m0)
```

```
Initial (logit-scale):
```

| Estimate | SE | z | P(> z) |
|----------|-------|---------|---------|
| -0.00337 | 0.236 | -0.0143 | 0.989 |

```
Colonization (logit-scale):
```

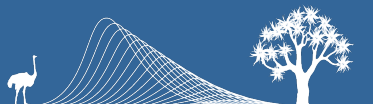
| Estimate | SE | z | P(> z) |
|----------|-------|-------|----------|
| -1.7 | 0.195 | -8.71 | 3.01e-18 |

```
Extinction (logit-scale):
```

| Estimate | SE | z | P(> z) |
|----------|-------|-------|---------|
| 0.214 | 0.318 | 0.672 | 0.502 |

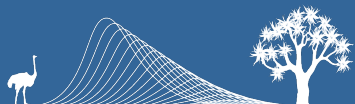
```
Detection (logit-scale):
```

| Estimate | SE | z | P(> z) |
|----------|------|-------|----------|
| -0.654 | 0.17 | -3.86 | 0.000115 |



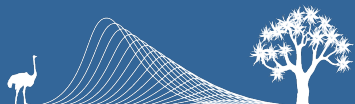
Parameter estimates

- ▶ $\text{logit}(\Psi_1) = -0.0034$
- ▶ What is Ψ_1 ? (Should be 0.6?)



Parameter estimates

- ▶ $\text{logit}(\Psi_1) = -0.0034$
- ▶ What is Ψ_1 ? (Should be 0.6?)
- ▶ $\Psi = \frac{e^{-0.0034}}{1+e^{-0.0034}}$
- ▶ $> \text{exp}(-0.00337) / (1+\text{exp}(-0.00337))$
[1] 0.4991575



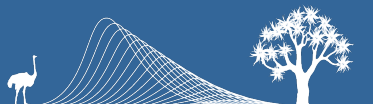
Parameter estimates

```
> names(m0)
[1] "psi" "col" "ext" "det"
```

```
> backTransform(m0, type="psi")
```

| Estimate | SE |
|----------|--------|
| 0.499 | 0.0591 |

```
> confint(backTransform(m0, type="psi"))
      0.025      0.975
0.3854436 0.6129562
```



Derived parameters

$$\Psi_t = \Psi_{t-1} \times (1 - \epsilon_{t-1}) + (1 - \Psi_{t-1}) \times \gamma_{t-1}$$

```
> backTransform(m0, type="ext")
```

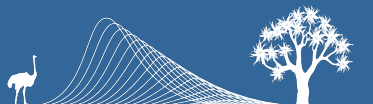
```
Estimate      SE  
0.553 0.0786
```

```
> backTransform(m0, type="col")
```

```
Estimate      SE  
0.154 0.0255
```

```
> m0@projected.mean
```

| | 1 | 2 | 3 | 4 | 5 |
|------------|-----------|-----------|-----------|-----------|----------|
| unoccupied | 0.5008437 | 0.6997875 | 0.7580149 | 0.7750571 | 0.780045 |
| occupied | 0.4991563 | 0.3002125 | 0.2419851 | 0.2249429 | 0.219955 |

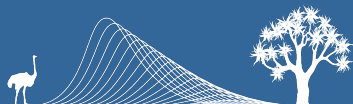
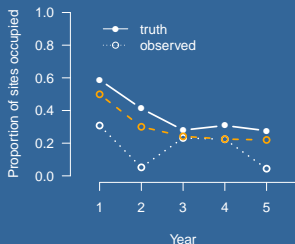


Will occupancy decrease forever?

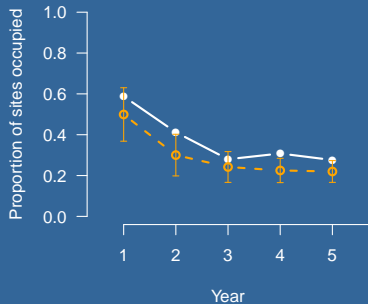
With constant γ and ϵ occupancy heading for an equilibrium:

$$\Psi_E = \frac{\gamma}{\gamma + \epsilon}$$

$$\hat{\Psi}_E = \frac{0.154}{0.154 + 0.553} = 0.218$$



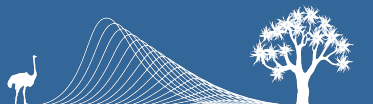
Confidence intervals for derived parameters



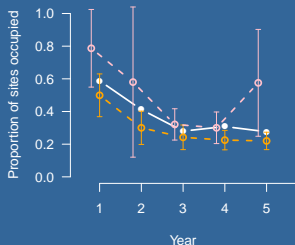
```
> m0 <- nonparboot(m0, B = 1000)
```

```
> cbind(projected=projected(m0)[2,],  
        SE=m0@projected.mean.bsse[2,])
```

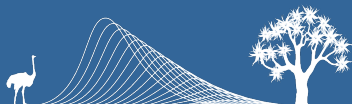
| | projected | SE |
|---|-----------|------------|
| 1 | 0.4991563 | 0.06678017 |
| 2 | 0.3002125 | 0.05202317 |
| 3 | 0.2419851 | 0.03846406 |
| 4 | 0.2249429 | 0.03041457 |
| 5 | 0.2199550 | 0.02719051 |



Yearly site covariates



```
> m1 <- colext(psiformula= ~1,  
+             gammaformula = ~ year,  
+             epsilonformula = ~ year,  
+             pformula = ~ year,  
+             data = simUMF)
```

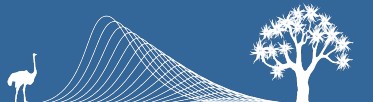


Model selection

```
> AIC(m0,m1)
Error in UseMethod("logLik") :
  no applicable method for 'logLik' applied to an object
  of class "c('unmarkedFitColExt', 'unmarkedFit')"
```

```
> models <- fitList(' psi(.)gam(.)eps(.)p(.)' = m0,
+                   ' psi(.)gam(Y)eps(Y)p(Y)' = m1)
> (ms <- modSel(models))
```

| | nPars | AIC | delta | AICwt | cumltvWt |
|------------------------|-------|---------|--------|---------|----------|
| psi(.)gam(Y)eps(Y)p(Y) | 14 | 1444.53 | 0.00 | 1.0e+00 | 1.00 |
| psi(.)gam(.)eps(.)p(.) | 4 | 1556.16 | 111.63 | 5.8e-25 | 1.00 |



Key references

- ▶ MacKenzie, D. I., J. D. Nichols, J. E. Hines, M. G. Knutson, and A. B. Franklin. 2003. Estimating site occupancy, colonization, and local extinction when a species is detected imperfectly. *Ecology* 84:2200-2207. **This paper introduced dynamic occupancy models.**
- ▶ Weir, L. A., I. J. Fiske, and J. A. Royle. 2009. Trends in Anuran Occupancy from Northeastern States of the North American Amphibian Monitoring Program. *Herpetological Conservation and Biology* 4:389-402. **Early application with detailed description.**
- ▶ Ian Fiske, Richard Chandler (2011). unmarked: An R Package for Fitting Hierarchical Models of Wildlife Occurrence and Abundance. *Journal of Statistical Software*, 43(10), 1-23. URL <http://www.jstatsoft.org/v43/i10/>. **This paper introduced unmarked package; see also package vignettes.**
- ▶ Bailey, L. L., D. I. MacKenzie, and J. D. Nichols. 2014. Advances and applications of occupancy models. *Methods in Ecology and Evolution* 5:1269-1279. **Concise overview of occupancy models.**
- ▶ MacKenzie, D. I., J. D. Nichols, J. A. Royle, K. H. Pollock, L. L. Bailey, and J. E. Hines. 2017. *Occupancy Estimation and Modeling: Inferring Patterns and Dynamics of Species Occurrence*. Academic Press. **The bible of occupancy modelling.**

